# Alabama Statewide Math Contest - Round 3 Division Two 

University of North Alabama

April 15, 2023

## Scoring

## Scoring

$$
\begin{array}{rr}
0: 00-0: 30 & 10 \text { points } \\
0: 31-1: 00 & 8 \text { points } \\
\text { 1:01-1:30 } & 6 \text { points } \\
1: 31-2: 00 & 4 \text { points }
\end{array}
$$

If the first person to answer is correct, they receive 2 Bonus Points.

## Rules

## Rules

1. Answers must be in answer box provided to be counted. Units such as cm, in, etc. are not necessary.
2. Fractions must be reduced. Improper fractions are acceptable.
3. The numbers $\pi$ and $e$ must be left as such.
4. Complex numbers must be put into $a+b i$ form.

## Rules

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5. Answers with radicals must be simplified. Denominators must be rationalized.
6. Exponents should be positive.
7. Answers involving trigonometric functions should be simplified as much as possible.
8. $\log (x)$ means $\log _{10}(x)$ and $\ln (x)$ means $\log _{e}(x)$.
9. The time limit for all problems is 2 minutes.

## Sample Problem \# 1

## Sample Problem

$\square$

Solve for $x$ in the equation

$$
x^{2}-6 x-3=0
$$

## Sample Problem

## Answer:

## Sample Problem

Answer: $3+2 \sqrt{3}$, and $3-2 \sqrt{3}$.

## Round 3

## Geometry

## Geometry Question \# 1

## Geometry Question \# 1

$\square$
What is the area of a triangle with side lengths 7,7 , and 10 ?

## Geometry Question \# 1

## Answer:

## Geometry Question \# 1

Answer: $10 \sqrt{6}$

## Geometry Question \# 2

## Geometry Question \# 2

$\square$
The point $(2,6)$ is reflected about the line $x=-2$ and then about the line $y=x$. What is the resultant point?

## Geometry Question \# 2

## Answer:

## Geometry Question \# 2

## Answer: $(6,-6)$

## Round 3

## Algebra II

## Algebra II Question \# 3

## Algebra II Question \# 3



If $f(x)=x^{2}-2 x+4$, solve $f(2 x)=4 f(x)$ for $x$.

## Algebra II Question \# 3

Answer:

## Algebra II Question \# 3

## Answer: 3

## Algebra II Question \# 4

## Algebra II Question \# 4



Find the solution to $(33-6 x)^{-1 / 5}-2=-1$.

## Algebra II Question \# 4

## Answer:

## Algebra II Question \# 4

## Answer: $\frac{16}{3}$

## Round 3

## Comprehensive Part 1

## Comprehensive Part 1 Question \# 5

## Comprehensive Part 1 Question \# 5



A bag contains 4 Blue, 4 Green, 4 Red, and 4 Yellow tiles. If you select 2 at random without replacement, what is the probability that neither tile is red?

## Comprehensive Part 1 Question \# 5

## Answer:

## Comprehensive Part 1 Question \# 5

## Answer: $\frac{11}{20}$

## Comprehensive Part 1 Question \# 6

## Comprehensive Part 1 Question \# 6



The graph of the parabola $y=a x^{2}+b x+c$ goes through points $(-2,-3),(0,-1)$, and $(2,9)$. What is the value of $a+b+c$ ?

## Comprehensive Part 1 Question \# 6

Answer:

## Comprehensive Part 1 Question \# 6

Answer: 3

## Round 3

## Comprehensive Part 2

## Comprehensive Part 2 Question \# 7

## Comprehensive Part 2 Question \# 7



Find the largest solution to $\cos ^{4} x-\sin ^{4} x=0$ on $[0,2 \pi)$.

## Comprehensive Part 2 Question \# 7

## Answer:

## Comprehensive Part 2 Question \# 7

## Answer: <br> $$
\frac{7 \pi}{4}
$$

## Comprehensive Part 2 Question \# 8

## Comprehensive Part 2 Question \# 8

$\square$
Find the distance between the two foci of the ellipse $\frac{x^{2}}{9}+\frac{y^{2}}{25}=1$.

## Comprehensive Part 2 Question \# 8

## Answer:

## Comprehensive Part 2 Question \# 8

Answer: 8

## Round 3

## Team

## Team Question \# 9

## Team Question \# 9



Find the largest solution to the equation $16^{x^{2}+3 x-1}=8^{x^{2}+3 x+2}$.

## Team Question \# 9

Answer:

## Team Question \# 9

## Answer: 2

## Team Question \# 10

## Team Question \# 10

$\square$
How many vertical asymptotes does the graph of the function

$$
f(x)=\frac{(x-2) \sin x}{\cos x}
$$

have on $[0,100 \pi)$ ?

## Team Question \# 10

## Answer:

## Team Question \# 10

## Answer: 100

## End of Round 3

